$\qquad$

## The Equation of a Line in Slope $y$-intercept Form: $y=m x+b$

In the previous unit, we learned that a partial variation represents a linear relation with the form $y=m x+b$. We concluded:

A diagonal line has an equation in the form of $y=m x+b$ where $m$ is the $\qquad$ and $b$ is the $\qquad$ . A line sloping down towards the right has a slope whereas a line sloping up towards the right has a $\qquad$ slope. The value of the slope is the $\qquad$ of $x$.

Example A: Graph the lines $y=3 x+2$ and $y=-\frac{1}{2} x+5$


Steps on Graphing Lines

1. Plot the $y$-intercept.
2. Start at the $y$-intercept and plot two more points using the slope.

Remember:
(i) a negative rise means you travel down from the y-intercept.
(ii) A negative run means you travel left from the y-intercept.

Example B: Consider $y=-\frac{1}{2} x+5$, do the points $(4,3)$ and $(-6,8)$ lie on the line? Justify your answer in more than 1 way.

Example C: Given the graphs below, determine their equations.


Vertical Line:

## Key Concepts

2
All horizontal lines always have a slope of $\qquad$ because the rise $=$ $\qquad$ .

The equation $y=m x+b$ becomes

$$
y=b \quad \text { because } m=
$$

Another way of thinking about it is:
All the coordinates on the line have the same $y$-value and different $x$ values, thus $y=b=y$-intercept.


3
All vertical lines always have an $\qquad$ slope
because the $\qquad$ $=0$. You cannot divide by 0 .

This equation does not follow the form $y=m x+b$.
$\Rightarrow \Rightarrow$ The equation is in the form $x=L$, where $L$ is the number that crosses the $x$-axis since all the $x$-values on the line are the same.


Example C: Graph the lines $y=2$ and $x=-1$ on the grids above.
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Example D: State the equation of each line below.


Example E: Given the value of the slope and y-intercept, determine the equation of the line for each set.

|  | $m$ | $b$ | Equation | Type of Line |
| :--- | :---: | :---: | :---: | :---: |
| (i) | -2 | 5 |  |  |
| (ii) | 0 | 7 |  |  |
| (iii) | $\frac{4}{3}$ | -2 |  |  |
| (iv) | $-\frac{1}{2}$ | 0 |  |  |

Using the equation from question $D$ (iii), does the point $(-6,-10)$ satisfy the equation? Show your work algebraically.

Example E: If they exist, find the slope and $y$-intercept for each equation given in the table below then graph all the lines on the grid provided. Show at least three points on the line.

|  | Equation | $m$ | $b$ |
| :--- | :---: | :---: | :---: |
| (i) | $y=\frac{x}{4}-5$ |  |  |
| (ii) | $y=8-3 x$ |  |  |
| (iii) | $y=\frac{2}{3} x-1$ |  |  |
| (iv) | $y=-4$ |  |  |
| (v) | $x=-7$ |  |  |



## Example F:

A) Identify the slope and the vertical intercept of each linear relation and explain what they mean.
B) Write an equation to describe the relationship.
C) Identify the $x$-intercept and interpret its meaning.


